

Class VIII Session 2024-25
Subject - Mathematics
Sample Question Paper - 4

Time Allowed: 3 hours



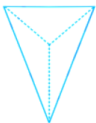
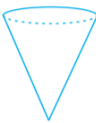
Maximum Marks: 80

General Instructions:

1. This Question Paper has 4 Sections A-D.
2. Section A has 20 MCQs carrying 1 mark each.
3. Section B has 6 questions carrying 02 marks each.
4. Section C has 8 questions carrying 03 marks each.
5. Section D has 6 questions carrying 04 marks each.
6. All Questions are compulsory.
7. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated

Section A

- The number which is neither positive nor negative is [1]
 - 0
 - 5
 - 1
 - 10
- If $x + 0 = 0 + x = x$, which is rational number, then 0 is called [1]
 - multiplicative inverse of x
 - additive inverse of x
 - reciprocal of x
 - identity for addition of rational numbers
- Solve: $\frac{x-4}{3} + \frac{2x-3}{35} = \frac{5x-32}{9} - \frac{x+9}{28}$ [1]
 - 19
 - 5
 - 10
 - 20
- Solve: $2y + \frac{5}{3} = \frac{26}{3} - y$ [1]
 - $\frac{7}{3}$
 - 7
 - 3
 - $\frac{5}{3}$
- What is the sum of the measures of the angles of a convex quadrilateral? [1]
 - 90°
 - 45°
 - 180°
 - 360°
- The three angles of any quadrilateral is 105° , 120° and 75° respectively, the fourth angle is [1]
 - 75°
 - 50°
 - 60°
 - 70°

7. Which of the following would end with digit 1? [1]
- A. 49^2
 B. 23^2
 C. 54^2
 D. 67^2
- a) D
 b) A
 c) C
 d) B
8. What is the value of $\sqrt{1522756}$? [1]
- a) 2434
 b) 1234
 c) 1232
 d) 1324
9. If one side of a cube is 33 m, then the volume of the cube is [1]
- a) 35936
 b) 3934
 c) 39753
 d) 35937
10. Find the smallest number by which 8788 must be divided so that the quotient will be a perfect cube. [1]
- a) 4
 b) 5
 c) 3
 d) 6
11. A table marked at Rs 15,000 is available for Rs 14,400. Find the discount percent. [1]
- a) 3%
 b) 5%
 c) 6%
 d) 4%
12. The compound interest on ₹ 30000 at 7% per annum is ₹ 4347. The period (in years) is: [1]
- a) 3
 b) 2
 c) $2\frac{1}{2}$
 d) 4
13. Add: $a - b + ab$, $b - c + bc$, $c - a + ac$ [1]
- a) $ab + bc + ac$
 b) $ab + bc$
 c) $a + b + c$
 d) abc
14. Which of the following 3-dimensional figures has the top, side and front as triangles? [1]
- a) 
 b) 
 c) 
 d) 
15. A metallic cylindrical pipe has outer radius of 3 cm and an inner radius of 2 cm. If the length of the pipe is 70 cm, then the volume of metal in the pipe, in cm^3 , is [1]
- a) 280π
 b) 630π

- c) 910π d) 350π
16. If $3^x = \frac{1}{9}$, the value of x is [1]
- a) 1 b) -2
- c) 2 d) $\frac{1}{2}$
17. $\left(\frac{x^{-3}}{y^3}\right)^{2/3} \times \left(\frac{x^3}{y^{-3}}\right)^{-2/3}$ is equal to [1]
- a) $\frac{1}{x^2y^2}$ b) $\frac{y^4}{x^{-4}}$
- c) $\frac{x^4}{y^{-4}}$ d) $\frac{x^{-4}}{y^4}$
18. x and y are in inverse proportion. When x = 12, y = 3. Which of the following is not a possible pair of corresponding values of x and y? [1]
- a) 5 and 6 b) 10 and 3.6
- c) 4 and 9 d) 72 and 0.5
19. The factorisation of $x^2 + x + xy + y + zx + z$ is. [1]
- a) $(x + y + z)(z + x)$ b) $(x + y + z)(x + y)$
- c) $(x + y + z)(y + z)$ d) $(x + y + z)(x + 1)$
20. Factorise: $169a^2 - 144b^2$ [1]
- a) $(13a + 12b)$ b) $(13a - 12b)$
- c) $(12a - 13b)$ d) $(13a + 12b)(13a - 12b)$

Section B

21. Solve: $x + 7 - \frac{8x}{3} = \frac{17}{6} - \frac{5x}{2}$ [2]

OR

Solve: $0.16(5x - 2) = 0.4x + 7$

22. How many sides does a regular polygon have if the measure of an exterior angle is 24° ? [2]
23. Shoes of the following brands are sold in November 2007 at a shoe store. Construct a pie chart for the given data. [2]

| Brand | Number of pairs of shoes sold |
|-------|-------------------------------|
| A | 130 |
| B | 120 |
| C | 90 |
| D | 40 |
| E | 20 |

24. Is 68600 a perfect cube? If not, find the smallest number by which 68600 must be multiplied to get a perfect cube? [2]

OR

Find out if 6859 is a perfect cube?

25. Simplify $3x(4x - 5) + 3$ and find its values for [2]
- i. $x = 3$

ii. $x = \frac{1}{2}$

26. The distance between school and house of a girl is given by 5 cm in a picture, using the scale 1cm: 5 km. Find the actual distance between the two places? [2]
27. Find $\frac{-4}{5} \times \frac{3}{7} \times \frac{15}{16} \times \left(\frac{-14}{9}\right)$ [3]

OR

Four friends had a competition to see how far could they hop on one foot. The table given shows the distance covered by each.

| Name | Distance covered (in km) |
|-------|--------------------------|
| Seema | $\frac{1}{25}$ |
| Nancy | $\frac{1}{32}$ |
| Megha | $\frac{1}{40}$ |
| Soni | $\frac{1}{20}$ |

- a. How farther did Soni hop than Nancy?
- b. What is the total distance covered by Seema and Megha?
- c. Who walked farther, Nancy or Megha?
28. Solve the linear equation $\frac{x-5}{3} = \frac{x-3}{5}$. [3]
29. Find the smallest number by which 1620 must be divided to get a perfect square. [3]
30. The cost of 5 oranges is ₹ 75 and the cost of 6 apples is ₹ 78. Which fruit is costlier and why? [3]

OR

The cost price of an article is ₹375. Find the marked price of the article so as to gain 8%, after allowing a discount of 25%?

31. Find the sum of $4x^2 - 3x + 2$ and $3x^2 + 4x - 8$. [3]
32. Daniel is painting the walls and ceiling of a cuboidal hall with length, breadth and height of 15 m, 10 m and 7 m respectively. From each can of paint 100 m² of area is painted. How many cans of paint will she need to paint the room? [3]
33. A light-year is a distance that light can travel in one year. [3]
1 light year = 9,460,000,000,000 km.
- a. Express one light-year in scientific notation.
- b. The average distance between Earth and Sun is 1.496×10^8 km.
- Is the distance between Earth and the Sun greater than, less than or equal to one light-year?



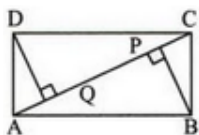
34. Factorise: $a^4 - 2a^2b^2 + b^4$ [3]
35. ABCD is a trapezium such that $AB \parallel CD$, $\angle A : \angle D = 2 : 1$, $\angle B = \angle C = 7 : 5$. Find the angles of the trapezium. [4]

OR

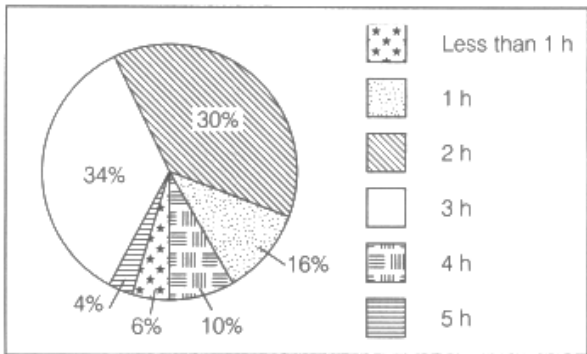
In the given rectangle ABCD, BP and DQ are perpendiculars to AC from B and D respectively/ Answer the following and give reasons for your answers.

- i. Is $AD = BC$?
- ii. Is $\angle BAP = \angle DCQ$?

- iii. Is $\triangle DAQ \cong \triangle BCP$?
- iv. Is $BP = DQ$?



36. Given below is a pie chart showing the time spend by a group of 350 children in different games. Observe it and answer the questions that follow. [4]
- a. How many children spend atleast one hour in playing games?
 - b. How many children spend more than 2 h in playing games?
 - c. How many children spend 3 or lesser hours in playing games?
 - d. Which is greater, number of children who spend 2 hours or more per day or number of children who play for less than one hour?



37. Arunima bought household items whose marked price and discount % is as follows [4]

| Item | Quantity | Rate (in ₹) | Discount% |
|----------------|----------|-------------|-----------|
| (i) Atta | 1 packet | 200 | 16% |
| (ii) Detergent | 1 packet | 371 | 22.10% |
| (ii) Namkeen | 1 packet | 153 | 18.30% |

Find the total amount of the bill she has to pay.

OR

A sum of money becomes ₹ 17,640 in 2 years and ₹ 18,522 in 3 years at the same rate of interest compounded annually. Find the rate of interest.

38. The length , width and height of a cuboid are 10cm, 8 cm and 7 cm respectively . Find the lateral surface area of a cuboid? [4]
39. Suppose 2 kg of sugar contains 9×10^6 crystals. How many sugar crystals are there in [4]
- (i) 5 kg of sugar ?
 - (ii) 1.2 kg of sugar ?
40. Ajit can ride a scooter constantly at a speed of 30 kms/hour. Draw a time-distance graph for this situation. Use it to find [4]
- i. the time taken by Ajit to ride 75 km.
 - ii. the distance covered by Ajit in $3\frac{1}{2}$ hours.

Solution

Section A

1. (a) 0

Explanation: 0 is neither positive nor negative.

2.

(d) identity for addition of rational numbers

Explanation: We know that, the sum of any rational number and zero (0) is the rational number itself. Now, $x + 0 = 0 + x = x$, which is a rational number, then 0 is called identity for addition of rational numbers.

3. (a) 19

Explanation: $\frac{x-4}{3} + \frac{2x-3}{35} = \frac{5x-32}{9} - \frac{x+9}{28}$

Multiplying throughout by 9, we have

$3x - 12 + \frac{18x-27}{35} = 5x - 32 - \frac{9x+81}{28}$ transposing,

$\frac{18x-27}{35} + \frac{9x+81}{28} = 2x - 20$

Now clear of fractions by multiplying by

$5 \times 7 \times 4$ or 14

thus $72x - 108 + 45x + 405 = 280x - 2800$

$\therefore 2800 - 108 + 405 = 280x - 72x - 45x$

$\therefore 3097 = 163$

$\therefore x = 19$

4. (a) $\frac{7}{3}$

Explanation: $2y + \frac{5}{3} = \frac{26}{3} - y$

or, $2y + y = \frac{26}{3} - \frac{5}{3}$

or, $3y = \frac{21}{3}$

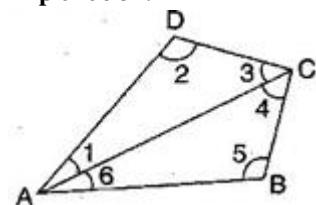
or, $3y = 7$

or, $y = \frac{7}{3}$

5.

(d) 360°

Explanation:



Let ABCD is a convex quadrilateral, then we draw a diagonal AC which divides the quadrilateral into two triangles.

$\angle A + \angle B + \angle C + \angle D$

$= \angle 1 + \angle 6 + \angle 5 + \angle 4 + \angle 3 + \angle 2$

$= \angle(1 + 2 + 3) + \angle(4 + 5 + 6)$

We are aware that the total sum of the interior angles of any triangle will be 180° and a quadrilateral is made up of two triangles

Thus, the sum of the interior angles of both the triangles are $180 + 180 = 360^\circ$

So, the sum of the measures of the angles of a convex quadrilateral is 360°

6.

(c) 60°

Explanation: Let the sum of all four angles of rhombus = 360°

A/q

The three angles of quadrilateral is $105^\circ, 120^\circ, 75^\circ$
 The measurement of fourth angle = $360^\circ - (105^\circ + 120^\circ + 75^\circ)$
 $= 360^\circ - 300^\circ = 60^\circ$

7.

(b) A

Explanation: The answer is 49^2 as here the unit's digit is 9 and $9^2 = 81$ where the unit's digit is 1, so 49^2 would end with digit 1.

8.

(b) 1234

Explanation: From the prime factorization of $\sqrt{1522756}$ we get 1234.

9.

(d) 35937

Explanation: Volume of cube = $(33)^3 = 35937$

10. (a) 4

Explanation: $8788 = 2 \times 2 \times 13 \times 13 \times 13$

Therefore, by above calculation we get that if 8788 is divided by 4 then it gives a perfect cube.

11.

(d) 4%

Explanation: Discount = $\frac{\text{Markedprice} - \text{Sellingprice}}{\text{Markedprice}} \times 100$
 $= \frac{15,000 - 14,400}{15,000} \times 100$
 $= \frac{600 \times 100}{15,000}$
 $= 4\%$

12.

(b) 2

Explanation: P = ₹ 30000, r = 7% P.a., C.I = ₹ 4347,

n = ?

\Rightarrow Amount = ₹ 30000 + ₹ 4347 = ₹ 34347

$\therefore 34347 = 30000 \left(1 + \frac{7}{100}\right)^n$

$\Rightarrow \left(\frac{107}{100}\right)^n = \frac{34347}{30000} = \frac{11449}{10000}$

$\Rightarrow \left(\frac{107}{100}\right)^n = \left(\frac{107}{100}\right)^2 \Rightarrow n = 2$

13. (a) $ab + bc + ac$

Explanation: $(a - b + ab) + (b - c + bc) + (c - a + ac)$

opening brackets we get,

$a - b + ab + b - c + bc + c - a + ac$

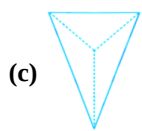
solving like terms and unlike terms we get,

$a - a - b + b - c + c + ab + bc + ac$

$0 + 0 + 0 + ab + bc + ac$

$ab + bc + ac$

14.



Explanation: 3-dimensional figures has the top, side and front as triangles name as a triangular pyramid.

15.

(d) 350π

Explanation: According to the question,

Outer radius (r_1) of pipe = 3 cm

inner radius (r_2) of pipe = 2 cm

length of pipe (h) = 70 cm

\therefore Volume of metal in the pipe = $\pi(r_1^2 - r_2^2) \times h$

$$= \pi(3^2 - 2^2) \times 70$$

$$= \pi(9 - 4) \times 70$$

$$= \pi \times 5 \times 70 = 350\pi \text{ cm}^3$$

16.

(b) -2

Explanation: $\because 3^x = \frac{1}{9}$

$$\therefore 3^x = \left(\frac{1}{3}\right)^2$$

$$\text{or } 3^x = 3^{-2}$$

On comparing both sides, we get $x = -2$

17.

(d) $\frac{x^{-4}}{y^4}$

Explanation: $\frac{x^{-4}}{y^4}$

18. (a) 5 and 6

Explanation: For inverse proportion, $xy = \text{constant}$ or $x_1y_1 = x_2y_2$

$$\text{As, } x_1y_1 = 36; x_2y_2 = 5 \times 6 = 30$$

$$\therefore x_1y_1 \neq x_2y_2$$

19.

(d) $(x + y + z)(x + 1)$

Explanation: $x^2 + x + xy + y + zx + z$

$$= x(x + 1) + y(x + 1) + z(x + 1)$$

$$= (x + 1)(x + y + z)$$

20.

(d) $(13a + 12b)(13a - 12b)$

Explanation: $169a^2 - 144b^2$

$$(13a)^2 - (12b)^2$$

$$(13a + 12b)(13a - 12b)$$

Section B

$$\begin{aligned} 21. x + 7 - \frac{8x}{3} &= \frac{17}{6} - \frac{5x}{2} \\ \Rightarrow \frac{x}{1} - \frac{8x}{3} + \frac{5x}{2} &= \frac{17}{6} - \frac{7}{1} \\ \Rightarrow \frac{6x - 16x + 15x}{6} &= \frac{17 - 42}{6} \\ \Rightarrow \frac{5x}{6} &= \frac{-25}{6} \\ \Rightarrow x &= \frac{-25 \times 6}{6 \times 5} \\ \Rightarrow x &= -5 \end{aligned}$$

OR

$$\text{Given, } 0.16(5x - 2) = 0.4x + 7$$

$$\Rightarrow 0.8x - 0.32 = 0.4x + 7$$

$$\Rightarrow 0.8x - 0.4x = 0.32 + 7 \text{ [transposing } 0.4x \text{ to LHS and } -0.32 \text{ to RHS]}$$

$$\Rightarrow 0.4x = 7.32$$

$$\Rightarrow \frac{0.4x}{0.4} = \frac{7.32}{0.4} \text{ [dividing both sides by } 0.4]$$

$$\therefore x = 18.3$$

22. Let the number of sides be n, Then, $n(24^\circ) = 360^\circ$.

$$\Rightarrow n = \frac{360^\circ}{24^\circ} = 15$$

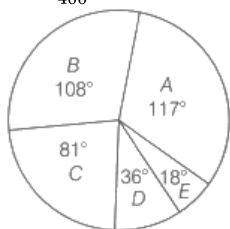
Hence, the number of sides is 15.

23. Total number of pairs of shoes sold = $(130 + 120 + 90 + 40 + 20) = 400$

\therefore Central angle of pie chart representing the brands:



- i. $A = \frac{130}{400} \times 360^\circ = 117^\circ$ (as total central angle = 360°)
 ii. $B = \frac{120}{400} \times 360^\circ = 108^\circ$
 iii. $C = \frac{90}{400} \times 360^\circ = 81^\circ$
 iv. $D = \frac{40}{400} \times 360^\circ = 36^\circ$
 v. $E = \frac{20}{400} \times 360^\circ = 18^\circ$



24. We have, $68600 = 2 \times 2 \times 2 \times 5 \times 5 \times 7 \times 7 \times 7$. In this factorisation, we find that there is no triplet of 5.

So, 68600 is not a perfect cube. To make it a perfect cube we multiply it by 5.

Thus, $68600 \times 5 = 2 \times 2 \times 2 \times 5 \times 5 \times 5 \times 7 \times 7 \times 7 = 343000$, which is a perfect cube.

Hence, the smallest number by which 68600 must be multiplied to get a perfect cube is 5.

OR

$$\begin{array}{r|l} 19 & 6859 \\ \hline 19 & 361 \\ \hline 19 & 19 \\ \hline & 1 \end{array}$$

By prime factorisation,

$6859 = \underline{19} \times \underline{19} \times \underline{19}$ [grouping the factors in triplets]

$= 19^3$ which is a perfect cube.

Therefore, 6859 is a perfect cube.

25. We have $3x(4x - 5) + 3$

simplification: $3x(4x - 5) + 3 = 3x(4x) - 3x(5) + 3 = 12x^2 - 15x + 3$

i. $x = 3$

Putting $x = 3$ in above equation, we get $12(3)^2 - 15(3) + 3$

$$= 12(9) - 45 + 3$$

$$= 108 - 42 = 66$$

ii. $x = \frac{1}{2}$

Putting $x = \frac{1}{2}$ in above equation, we get

$$12\left(\frac{1}{2}\right)^2 - 15\left(\frac{1}{2}\right) + 3$$

$$= 12 \times \frac{1}{4} - \frac{15}{2} + 3$$

$$= 3 - \frac{15}{2} + 3$$

$$= 6 - \frac{15}{2}$$

$$= \frac{12-15}{2}$$

$$= \frac{-3}{2}$$

26. Given scale = 1 cm : 5 km, i.e. 1 cm in picture = 5 km of actual distance

\therefore 5 cm in picture = 5×5 km

Hence, the actual distance between the two places is 25 km.

27. We have, $\frac{-4}{5} \times \frac{3}{7} \times \frac{15}{16} \times \left(\frac{-14}{9}\right)$

$$= \left(\frac{-4}{5} \times \frac{15}{16}\right) \times \left[\frac{3}{7} \times \left(\frac{-14}{9}\right)\right] \text{ [}\therefore \text{ using commutativity and associativity]}$$

$$= \frac{-3}{4} \times \left(\frac{-2}{3}\right)$$

$$= \frac{1}{2}$$

OR

We have, $\frac{1}{25}, \frac{1}{32}, \frac{1}{40}, \frac{1}{20}$

At first, we convert the numbers as like denominators.

| | |
|---|----------------|
| 2 | 25, 32, 40, 20 |
| 2 | 25, 16, 20, 10 |
| 2 | 25, 8, 10, 5 |
| 5 | 25, 4, 5, 5 |
| | 5, 4, 1, 1 |

Taking LCM of 25, 32, 40 and 20 = $2 \times 2 \times 2 \times 5 \times 5 \times 4 = 800$

we get,

$$\frac{1}{25} = \frac{1 \times 32}{25 \times 32} = \frac{32}{800}, \frac{1}{32} = \frac{1 \times 25}{32 \times 25} = \frac{25}{800}, \frac{1}{40} = \frac{1 \times 20}{40 \times 20} = \frac{20}{800} \text{ and } \frac{1}{20} = \frac{1 \times 40}{20 \times 40} = \frac{40}{800}$$

a. Soni hop more than Nancy = $\frac{40}{800} - \frac{25}{800} = \frac{40-25}{800} = \frac{15}{800} = \frac{3}{160}$

b. Total distance covered by Seema and Megha = $\frac{32}{800} + \frac{20}{800} = \frac{32+20}{800} = \frac{52}{800} = \frac{13}{200}$

c. It is clear that Nancy walked farther than Megha.

28. $\frac{x-5}{3} = \frac{x-3}{5}$

It is a linear equation since it involves linear expressions only.

$$\therefore \frac{x}{3} - \frac{5}{3} = \frac{x}{5} - \frac{3}{5}$$

$$\therefore \frac{x}{3} - \frac{x}{5} = -\frac{3}{5} + \frac{5}{3} \dots [\text{Transposing } \frac{x}{5} \text{ to L.H.S. and } -\frac{5}{3} \text{ to R.H.S.}]$$

$$\therefore \frac{5x-3x}{15} = \frac{25-9}{15}$$

$$\therefore \frac{2x}{15} = \frac{16}{15}$$

$$\therefore x = 8$$

this is the required solution.

Verification,

$$\text{L.H.S.} = \frac{8-5}{3} = \frac{3}{3} = 1$$

$$\text{R.H.S.} = \frac{8-3}{5} = \frac{5}{5} = 1$$

Therefore, L.H.S. = R.H.S.

29. The prime factorisation of 1620 is $1620 = 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 5$

We see that prime factor 5 has no pair. So, if we divide 1620 by 5, then we get

| | |
|---|------|
| 2 | 1620 |
| 2 | 810 |
| 3 | 405 |
| 3 | 135 |
| 3 | 45 |
| 3 | 15 |
| | 5 |

$$1620 \div 5 = 2 \times 2 \times 3 \times 3 \times 3 \times 3$$

Now each factor has a pair. Therefore, $\frac{1620}{5} = 324$ is a perfect square.

Thus the required smallest number is 5.

30. Cost of 5 oranges = ₹ 75

$$\text{Cost of 1 orange} = \frac{75}{5} = ₹15$$

$$\text{Cost of 6 apples} = ₹ 78$$

$$\text{Cost of 1 apples} = \frac{78}{6} = ₹13$$

As, $15 > 13$,

oranges are more costlier than apples.

OR

$$\text{C.P. of the article} = ₹ 375$$

$$\text{Gain} = 8\%$$

$$S.P. = \frac{100 + \text{Gain}\%}{100} \times C.P.$$

$$= \frac{100 + 8}{100} \times 375$$

$$= \frac{108}{100} \times 375 = ₹405$$

Let the marked price of the article be Rs. x

$$\text{Discount}\% = 25\%$$

$$\text{Discount} = \frac{25}{100} \times x = \frac{x}{4}$$

$$S.P. = M.P - \text{Discount}$$

$$405 = x - \frac{x}{4} = \frac{3x}{4}$$

$$x = \frac{4 \times 405}{3} = 4 \times 135$$

$$x = ₹ 540.$$

Therefore, the marked price of the article is ₹ 540.

$$\begin{aligned} 31. (4x^2 - 3x + 2) + (3x^2 + 4x - 8) &= 4x^2 - 3x + 2 + 3x^2 + 4x - 8 \\ &= 4x^2 + 3x^2 + 4x - 3x + 2 - 8 \\ &= (4 + 3)x^2 + (4 - 3)x + (2 - 8) \\ &= 7x^2 + x - 6 \end{aligned}$$

$$32. l = 15 \text{ m}$$

$$b = 10 \text{ m}$$

$$h = 7 \text{ m}$$

Surface area to be painted

$$= 2(l \times b + b \times h + h \times l) - l \times b$$

$$= 2(15 \times 10 + 10 \times 7 + 7 \times 15) \text{ m}^2 - (15 \times 10) \text{ m}^2$$

$$= 2(150 + 70 + 105) \text{ m}^2 - 150 \text{ m}^2$$

$$= 2(325) \text{ m}^2 - 150 \text{ m}^2$$

$$= 650 \text{ m}^2 - 150 \text{ m}^2$$

$$= 500 \text{ m}^2$$

∴ Number of cans needed

$$= \frac{\text{Surface area to be painted}}{\text{Area painted by 1 can}}$$

$$= \frac{500}{100}$$

$$= 5$$

Hence, she will need 5 cans to paint the room.

$$33. \text{ a. Given, 1 light year} = 9,460,000,000,000 \text{ km}$$

$$\text{For standard form} = 946 \times 10^{10} \text{ km} = \frac{946}{100} \times 10^{10} \times 100 \text{ km}$$

$$= 9.46 \times 10^{12} \text{ km}$$

$$\text{b. The average distance between Earth and Sun} = 1.496 \times 10^8 \text{ km}$$

$$\therefore \text{Distance between Earth and Sun} = \frac{1.496}{10000} \times 10^8 \times 10^4 \text{ km} = 0.0001496 \times 10^{12} \text{ km}$$

$$\text{Since, } 9.46 > 0.0001496$$

So, the distance between Earth and Sun-less than one light-year.

$$34. a^4 - 2a^2b^2 + b^4$$

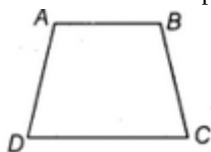
$$= (a^2)^2 - 2(a^2)(b^2) + (b^2)^2$$

$$= (a^2 - b^2)^2 \dots \text{[Using Identity II]}$$

$$= \{(a - b)(a + b)\}^2 \dots \text{[Using Identity III]}$$

$$= (a - b)^2(a + b)^2.$$

$$35. \text{ Let ABCD be a trapezium, where } AB \parallel CD.$$



Let the angles A and D be of measures $2x$ and x , respectively

$$\text{then } 2x + x = 180^\circ$$

[∵ in trapezium, the angles on either side of the base are supplementary]

$$\Rightarrow 3x = 180^\circ$$

$$\Rightarrow x = 60^\circ$$

$$\therefore \angle A = 2x = 60^\circ = 120^\circ, \angle D = 60^\circ$$

Again, let the angles B and C be $7x$ and $5x$ respectively. Then $7x + 5x = 180^\circ$

$$\Rightarrow 12x = 180^\circ$$

$$\Rightarrow x = 15^\circ$$

$$\text{Thus, } \angle B = 7 \times 15 = 105^\circ \text{ and } \angle C = 5 \times 15 = 75^\circ$$

OR

i. Yes (opposite sides of a rectangle)

ii. Yes, since, $AB \parallel CD$, AC is a transversal and they are alternate angles.

iii. Since DQ and BP are perpendiculars from D and B , respectively on AC , therefore, $\angle DQA = \angle BPC = 90^\circ$.

Thus $DQ \parallel BP$ (if the alternate angles are equal the lines are parallel)

Also $AD \parallel BC$ and AC is the transversal.

$$\therefore \angle DAQ = \angle BCP \text{ (Alternate angles)}$$

$$\text{Since } \angle DQA = \angle BPC \text{ and } \angle DAQ = \angle BCP,$$

$$\therefore \angle ADQ = \angle CBP$$

Now in $\triangle DAQ$ and $\triangle BCP$, we have

$$\angle DAQ = \angle BCP$$

$$\angle ADQ = \angle CBP$$

$$DA = BC$$

$$\therefore \triangle DAQ \cong \triangle BCP \text{ (by ASA condition of congruence)}$$

iv. Yes, (corresponding parts of congruent triangle $\triangle DAQ$ and $\triangle BCP$)

36. a. Number of children who spend atleast 1 h in playing games i.e. the number of children playing 1 h or more than 1 h

$$= (\text{Total number of children}) - (\text{Number of children spend less than 1 h})$$

$$= 350 - 6\% \text{ of } 350$$

$$= 350 - \frac{6}{100} \times 350$$

$$= 350 - 21 = 329$$

b. Number of children who spend more than 2 h in playing games

$$= (34 + 10 + 4)\% \text{ of the total number of students}$$

$$= 48\% \text{ of } 350$$

$$= \frac{48}{100} \times 350 = 168$$

c. Number of children who spend 3 or lesser hours in playing games

$$= (34 + 30 + 16 + 6)\% \text{ of total number of students}$$

$$= 86\% \text{ of } 350$$

$$= \frac{86}{100} \times 350 = 301$$

d. Number of children who spend 2 h or more per day in playing games

$$= (30 + 34 + 10 + 4)\% \text{ of total number of students}$$

$$= 78\% \text{ of total number of students}$$

Number of children who spend less than one hour = 6% of total number of students Clearly, number of children who play for 2 h or more per day is greater than the number of children who play for less than 1 h.

37. From the given data in the table,

$$\text{Rate of one packet of atta} = ₹200$$

$$\text{Discount \%} = 16\%$$

$$\text{So, price after discount} = 200 - \frac{16}{100} \times 200$$

$$= 200 - 32$$

$$= ₹168$$

$$\text{Rate of one packet of detergent} = ₹371$$

$$\text{Discount \%} = 22.10\%$$

$$\text{So, price after discount} = 371 - 371 \times \frac{22.10}{100}$$

$$= 371 - 81.991$$

$$= ₹289.009$$

$$\text{Rate of one packet of namkeen} = 153$$

$$\text{Discount \%} = 18.30\%$$

$$\text{So, price after discount} = 153 - 153 \times \frac{18.30}{100}$$

$$= 153 - 27.999$$

$$= 153 - 27.999$$

$$= ₹125.001$$

$$\therefore \text{Total bill amount to be paid} = ₹168 + ₹289.009 + ₹125.001$$

$$= ₹582.01$$

OR

Let Principal = P

Rate of Interest = R

$$\text{Amount}_1 (A_1) = ₹ 17,640$$

Time Period₁ (T_1) = 2 years

$$A_1 = P \left(1 + \frac{R}{100} \right)^{T_1}$$

$$17,640 = P \left(1 + \frac{R}{100} \right)^2$$

$$\text{Amount}_2 (A_2) = ₹ 18,522$$

Time Period₂ (T_2) = 3 years

$$A_2 = P \left(1 + \frac{R}{100} \right)^{T_2}$$

$$18,522 = P \left(1 + \frac{R}{100} \right)^3$$

$$\frac{A_1}{A_2} = \frac{18,522}{17,640} = \frac{P \left(1 + \frac{R}{100} \right)^3}{P \left(1 + \frac{R}{100} \right)^2}$$

$$\frac{21}{20} = \frac{\left(1 + \frac{R}{100} \right)^3}{\left(1 + \frac{R}{100} \right)^2} = 1 + \frac{R}{100}$$

$$\frac{21}{20} - 1 = \frac{R}{100}$$

$$R = \frac{21-20}{20} \times 100 = \frac{1}{20} \times 100 = 5\%$$

38. Here $l = 10$ cm, $w = 8$ cm and $h = 7$ cm

Using formula $LSA = 2h(l + w)$

$$= 2 \times 7(10 + 8)$$

$$= 14(18) = 252 \text{ cm}^2$$

39. Suppose the amount of sugar is x kg and the number of crystals is y

As the amount of sugar increases, the number of crystals also increases in the same ratio. It is a case of direct proportion. We

make use of the relation of the type $\frac{x_1}{y_1} = \frac{x_2}{y_2}$

(i) Here,

$$x_1 = 2$$

$$y_1 = 9 \times 10^6$$

$$x_2 = 5$$

Therefore, $\frac{x_1}{y_1} = \frac{x_2}{y_2}$ gives

$$\frac{2}{9 \times 10^6} = \frac{5}{y_2}$$

$$\therefore 2y_2 = 5 \times 9 \times 10^6$$

$$\therefore y_2 = \frac{5 \times 9 \times 10^6}{2}$$

$$\therefore y_2 = 22.5 \times 10^6$$

$$\therefore y_2 = 2.25 \times 10^7$$

Hence, there are 225×10^5 crystals.

(ii) Here,

$$x_1 = 2$$

$$y_1 = 9 \times 10^6$$

$$x_2 = 1.2$$

Therefore, $\frac{x_1}{y_1} = \frac{x_2}{y_3}$ gives

$$= \frac{2}{9 \times 10^6} = \frac{1.2}{y_3}$$

∴ 2y₃ = 1.2 × 9 × 10⁶

∴ 2y₃ = 10.8 × 10⁶

∴ y₃ = $\frac{10.8 \times 10^6}{2}$

∴ y₃ = 5.4 × 10⁶

Hence, these are 54 × 10⁵ crystals.

40.

| Hours of ride | Distance covered by scooter |
|---------------|-------------------------------|
| 1 hour | 1 × 30 km = 30 km |
| 2 hours | 2 × 30 km = 60 km |
| 3 hours | 3 × 30 km = 90 km |
| 4 hours | 4 × 30 km = 120 km and so on. |

We get a table of these values as follows:

| Time (in hours) | 1 | 2 | 3 | 4 |
|--------------------------|----|----|----|-----|
| Distance covered (in km) | 30 | 60 | 90 | 120 |

- i. Scale: (Fig) Horizontal: 2 units = 1 hour, Vertical: 1 unit = 10 km
- ii. Mark time on the horizontal axis.
- iii. Mark distance on the vertical axis.
- iv. Plot the points: (1, 30), (2, 60), (3, 90), (4, 120)
- v. Join the points. We get a linear graph.
 - a. Corresponding to 75 km on the vertical axis, we get the time to be 2.5 hours on the horizontal axis. Thus 2.5 hours are needed to cover 75 km.
 - b. Corresponding to 3½ hours on the horizontal axis, the distance covered is 105 km on the vertical axis.

